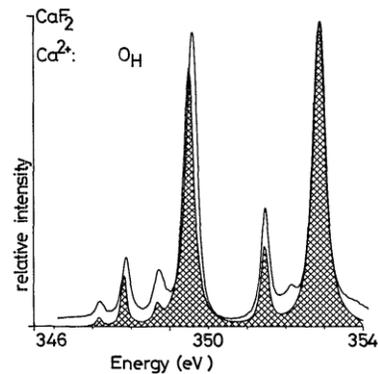
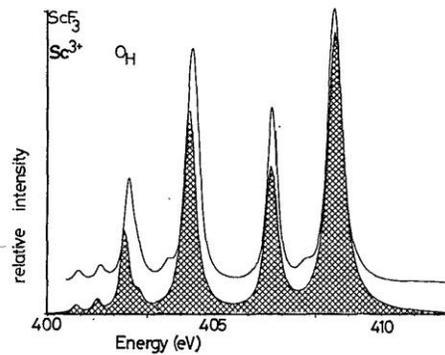
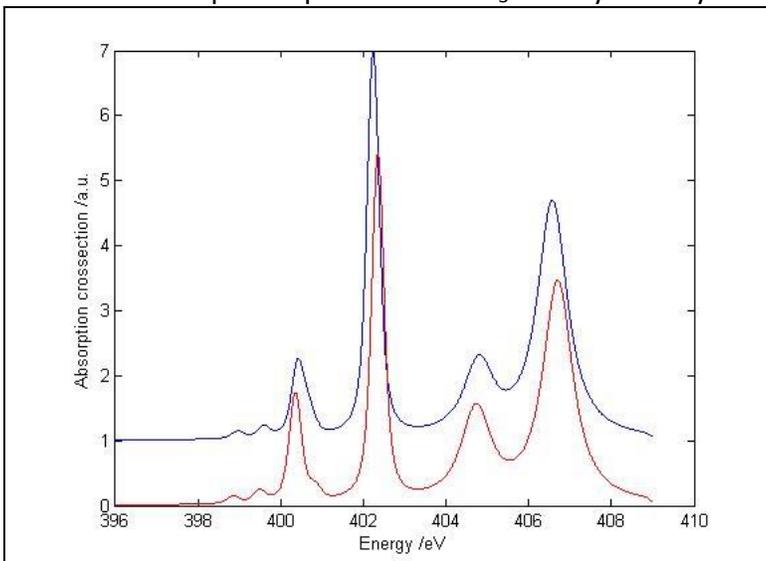


CTM4XAS: Discussion of tutorial exercises

Exercise crystal-1: The crystal field multiplet spectrum of ScF_3 and CaF_2



- a) Calculate the 2p XAS spectrum of ScF_3 . The symmetry is octahedral (O_h); optimise the value of $10Dq$.



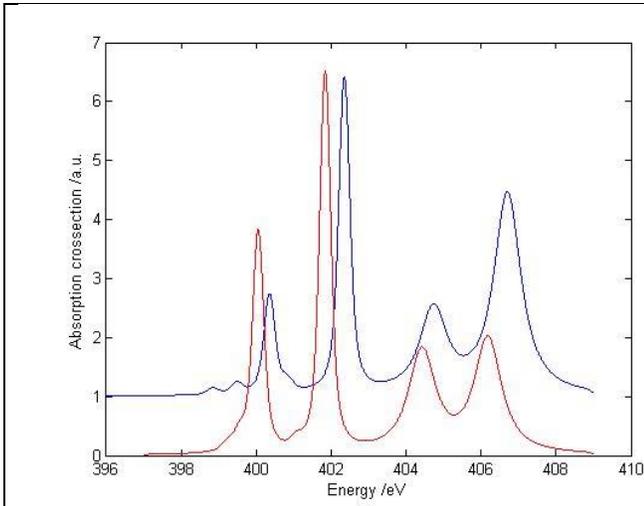
The blue spectrum has $10Dq = 1.5$.
The red spectrum has $10Dq = 1.8$.

To increase the correspondence with experiment the spectrum is split at 403 eV and the broadenings have been set to 0.1 Gaussian + 0.1 Lorentzian (0.4 Lorentzian above 403 eV).

>> to make a detailed simulation it is necessary to plot the experiment and theory on top of each other. (this will be improved in the next version of the exercises).

- b) How many peaks do you observe in the experiment and the calculation?
7 peaks in the calculation; in experiment 2 extra peaks are visible at 403 and 408 eV (these are due to surface peaks because the experiment was measured with electron yield)
- c) Reduce the Fdd Slater integral from 1.0 to 0.0. What is the effect on the spectrum? Explain.
There is no effect on the experiment. The ground state is $3d^0$ and has no 3d electrons filled, hence there are no 3d3d interactions.
- d) Reduce the Fpd and Gpd Slater integrals from 1.0 to 0.5. What is the effect on the spectrum? Explain.

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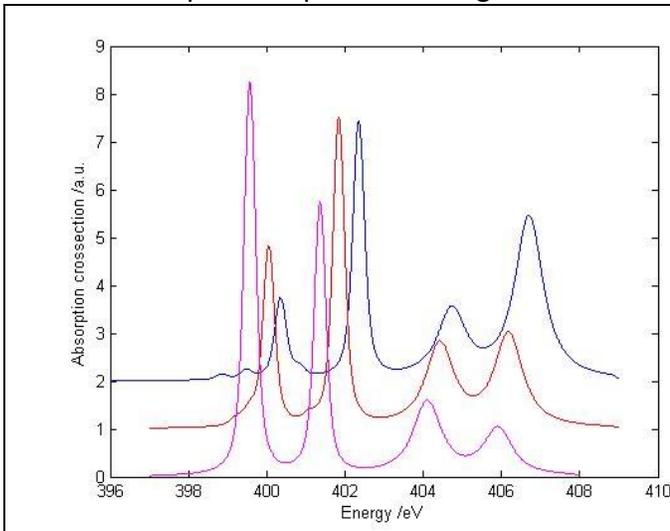


The blue spectrum is atomic.

The red spectrum has the Fpd and Gpd Slater integrals reduced to 50%.

The pre-peaks merge with the other peaks and the multiplet states come closer together and the spectrum starts to look like a single particle result.

e) Reduce the Fpd and Gpd Slater integrals to 0.0. What is the effect on the spectrum? Explain.



The bottom spectrum has all Slater integrals set to zero.

This is the single-particle spectrum with 4 peaks.

- The ratio between L3 and L2 is 4:2 following the degeneracy of the $2p_{3/2}$ and $2p_{1/2}$ states
- The ratio between the t_{2g} and e_g peaks is 3:2 following the number of states.
- This yields 4 peaks with relative intensities 6:4:3:2.

f) How many peaks are now visible? Explain the symmetry of all peaks. (see above) First peak is related to the t_{2g} states of the L3 edge. Then follow $eg-L3$, $t_{2g}-L2$ and $eg-L2$

g) Explain the number of peaks using atomic theory and the branching rules.

Atomic: $3d^0 \rightarrow 2p^5 3d^1$. Ground state is $1S_0$. Final state has $1P$, $1D$, $1F$, $3P$, $3D$ and $3F$ term symbols.

The number of term symbols with $J=0$ is equal to 1. There are 3 states with $J=1$, 4 states with $J=2$, 3 states with $J=3$ and 1 state with $J=4$. [Check that $1 \cdot (2 \cdot 0 + 1) + 3 \cdot 3 + 4 \cdot 5 + 3 \cdot 7 + 1 \cdot 9 = 1 + 9 + 20 + 21 + 9 = 60$, equal to the total number of states of a $2p$ and a $3d$ electron (i.e. $6 \cdot 10 = 60$)]

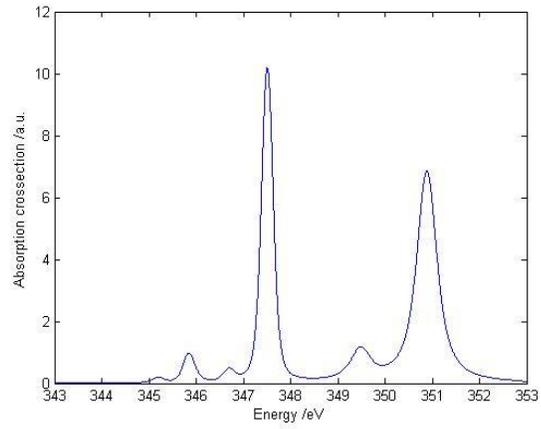
The atomic spectrum has 3 peaks (due to the selection rules the final state must have $J=1$)

Applying the branching rules (see reader), there will be 7 states in O_h symmetry.

h) Calculate the $2p$ XAS spectrum of CaF_2 . (Check first [on the web] the crystal structure of CaF_2 and the consequences for the local symmetry of Ca^{2+})

CaF_2 is cubic, i.e. the Ca^{2+} ion has 8 F^- neighbours. This implies that the t_{2g} and e_g states are inverted with respect to octahedral symmetry. This can be simulated with a negative $10Dq$ value. $10Dq = -0.9$ gives a good spectrum.

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The spectrum is split at 348 eV and the broadenings are 0.1 for Gaussian and 0.05 respectively 0.2 for Lorentzian.